Speeds of Sound, Densities, Isobaric Thermal Expansion, Compressibilities, and Internal Pressures of Heptan-1-ol, Octan-1-ol, Nonan-1-ol, and Decan-1-ol at Temperatures from (293 to 318) K and Pressures up to 100 MPa

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The speeds of sound in heptan-1-ol, octan-1-ol, and nonan-1-ol at pressures up to 101 MPa and in decan-1-ol at pressures up to 76 MPa have been measured within the temperature range of (293 to 318) K. The densities have been measured in the same temperature range under atmospheric pressure. The densities, isobaric heat capacities, isothermal compressibilities, isobaric thermal expansions, and internal pressures as functions of temperature and pressure have been calculated using the experimental results and the literature isobaric heat capacities for the atmospheric pressure. A modified method, based on the suggestion of Davis and Gordon (*J. Chem. Phys.* **1967**, *46*, 2650–2660), has been applied. The effect of pressure and temperature on the isothermal compressibility, isobaric thermal expansion, isobaric heat capacity, and internal pressure is discussed.

Introduction

Thermodynamic properties of simple organic liquids are of considerable interest from both the theoretical as well as the practical point of view. In the petrochemical industry, an important point of interest is the influence of "bio" additives to mineral fuels and greases such as alcohols or esters. Alkan-1ols belong to the liquids most frequently studied under atmospheric and also higher pressures. However, the thermodynamic and acoustic properties have been reported mainly for alcohols with 1 to 5 carbon atoms in the chain. Relatively few data are available in the literature^{1,2} for higher alkan-1-ols. Besides, the available results are rather incomplete. The speeds of sound in primary alcohols under elevated pressures have been measured by Sysoev and Otpuschennikov and published in Nauchnye Trudy (Kurskiœi Gosudarstvennyœi Pedagogicheskiœi Institute).² Unfortunately, these articles are not available. Khasanshin³ published a correlation equation for the speed of sound of akan-1-ols with the carbon atoms in the chain ranging from 4 to 12 for pressures from (0.1 to 100) MPa and for six temperatures from (303.15 to 453.15) K determined at 20 K steps. Plantier et al.⁴ reported the speed of sound in octan-1-ol at pressures up to 50 MPa and temperatures ranging from (303.15 to 373.15) K every 10 K. This work is a part of systematic studies of thermodynamic properties of organic liquids under elevated pressures using the acoustic method. Acoustic and thermodynamic properties of ethanol, propan-1ol, and hexan-1-ol at elevated pressures have been presented earlier.⁵⁻⁷ In this paper, new measurements of the speed of sound in heptan-1-ol, octan-1-ol, nonan-1-ol, and decan-1-ol in the temperature range from (293 to 318) K are reported. The speeds have been measured under pressures up to 101 MPa for heptan-1-ol, octan-1-ol, and nonan-1-ol and up to 76 MPa for decan-1-ol. The densities have been measured within the same temperature range under atmospheric pressure. The densities and isobaric heat capacities of heptan-1-ol, octan-1-ol, nonan-1-ol, and decan-1-ol for the temperature range from (293 to 318) K and at pressures up to 100 MPa for the first three alcohols

Table 1. Comparison of the Speeds of Sound and Densities
Obtained in This Work at $T = 298.15$ K under Atmospheric
Pressure with Those Reported in the Literature

		eporteu m	
component		exp.	lit.
heptan-1-ol	$u/m \cdot s^{-1}$	1327.27	1327.57,10 133011
•	$\rho/\text{kg}\cdot\text{m}^{-3}$	818.80	818.52, ¹² 818.78, ¹³ 818.9 ¹¹
octan-1-ol	$\rho/\text{m}\cdot\text{s}^{-1}$	1347.32	1347.18, ¹⁴ 1347.43, ¹⁵ 1347.5 ¹⁶
	$\rho/\text{kg}\cdot\text{m}^{-3}$	821.62	821.60,13 821.68,17 821.79,15 822.318
nonan-1-ol	$u/m \cdot s^{-1}$	1364.64	1364.41 , ¹⁹ 1364.70^{20}
	$\rho/\text{kg}\cdot\text{m}^{-3}$	824.24	824.02, ¹² 824.271, ²⁰ 824.47 ²¹
decan-1-ol	$u/m \cdot s^{-1}$	1379.69 ^a	1375.84, ¹⁵ 1380.2, ¹⁵ 1384 ¹⁵
	$\rho/\text{kg}\cdot\text{m}^{-3}$	826.37	826.23, ²⁰ 826.3, ¹⁵ 826.57, ¹⁵ 826.8 ¹⁸

^a Published in a previous work.²²

and up to 70 MPa for the latter one have been calculated using the speeds of sound under elevated pressures together with the densities and isobaric heat capacities at atmospheric pressure. To this end, the method based on the suggestion of Davis and Gordon⁸ with a numerical procedure proposed by Sun et al.⁹ was applied. Furthermore, the measured speeds of sound and calculated densities and isobaric heat capacities have been used for the calculation of the adiabatic and isothermal compressibilities, isobaric thermal expansion, and internal pressures. The effect of temperature and pressure on the isothermal compressibility, isobaric thermal expansion, isobaric heat capacity, and internal pressure is discussed. To the best of my knowledge, these properties have never been investigated in that pressure range.

Experimental Section

Chemicals. Heptan-1-ol was from Fluka with a minimum mass fraction 99 % of $C_7H_{15}OH$, octan-1-ol was from Lancaster with a minimum mass fraction 99 % of $C_8H_{17}OH$, nonan-1-ol was from Alfa Aesar with a minimum mass fraction 99 % of $C_9H_{19}OH$, and decan-1-ol was from Aldrich with a minimum mass fraction 99 % of $C_{10}H_{21}OH$. All the alcohols were dried over 0.3 nm molecular sieves. The concentration of water was determined by the Karl Fisher method. The mass fraction of water was less than 2·10⁻⁷ for nonan-1-ol and decan-1-ol and

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Table 2. S	Speed of Sound in	Alcohols Measured	at Pressures up	to 101 MPa v	within the	Temperature 1	Range of (2	293 to 318) H	ζ
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	heptan-1-ol			octan-1-ol			nonan-1-ol			dacan-1-ol	
T/K	p/MPa	$u/m \cdot s^{-1}$	<i>T</i> /K	p/MPa	$u/m \cdot s^{-1}$	<i>T</i> /K	p/MPa	$u/m \cdot s^{-1}$	<i>T</i> /K	p/MPa	$u/m \cdot s^{-1}$
292.89	0.10	1345.37	292.92	0.10	1365.25	292.88	0.10	1382.77	293.10	0.10	1397.23 ^a
292.78	15.20	1421.66	292.77	15.23	1440.32	292.87	15.20	1456.67	292.91	15.20	1470.57
292.77	30.39	1487.31	292.77	30.43	1505.21	292.87	30.39	1520.79	292.90	30.39	1533.84
292.77	45.59	1546.94	292.83	45.61	1564.06	292.86	45.59	1579.55	292.96	45.59	1592.01
292.77	60.79	1602.64	292.78	60.80	1619.26	292.87	60.79	1633.97	292.86	60.79	1646.34
292.76	75.99	1654.15	292.77	76.01	16/0.06	292.87	75.99	1684.39	298.07	0.10	1379.96
292.77	91.18	1701.99	292.79	91.20	1/1/.80	292.86	91.18	1/31.84	297.95	15.20	1453.77
292.77	101.32	1/32.68	292.83	96.12	1/32.99	292.86	101.32	1/62.05	297.96	30.39	1518.00
298.17	0.10	1327.21	298.20	0.10	1347.13	298.18	0.10	1304.30	297.98	45.59	15/0./0
298.00	20.20	1404.95	296.19	30.41	1422.39	297.90	30.30	1440.24	297.90	66.24	1640.80
298.00	30.39	14/1.//	296.15	50.41 45.61	1400.01	297.90	30.39	1505.59	297.93	60.24	1649.80
298.00	43.39	1588 18	298.09	60.84	1604.63	297.90	43.39	1610.08	297.90	71.85	1668.22
298.00	75.99	1640.40	298.07	76.04	1656 52	297.95	75.99	1670.69	297.99	73 52	1673.62
298.06	91.18	1688.89	298.07	91.19	1703.92	297.95	91.18	1718 71	297.99	74 70	1677.61
298.06	101.32	1719.64	298.07	97.84	1724 34	297.95	101.32	1749.18	298.00	75 99	1681 72
303.14	0.10	1310.24	303.18	0.10	1330.19	303.16	0.10	1347.52	303.04	0.10	1362.82^{a}
302.94	15.20	1389.45	303.27	15.20	1406.24	302.94	15.20	1424.28	302.92	15.20	1436.75
302.94	30.39	1457.34	303.28	30.41	1473.29	302.94	30.39	1490.24	303.08	30.39	1501.48
302.94	45.59	1518.74	303.27	45.60	1533.86	302.93	45.59	1550.12	303.11	45.59	1560.98
302.94	60.79	1575.32	303.26	60.82	1590.15	302.93	60.79	1606.05	303.02	60.79	1616.95
302.95	75.99	1628.00	303.15	76.00	1642.79	302.93	75.99	1657.58	303.03	66.24	1635.74
302.94	91.18	1676.97	303.16	91.20	1691.22	302.93	91.18	1705.79	303.05	69.23	1645.65
302.94	101.32	1708.00	303.20	101.34	1722.27	302.93	101.32	1736.67	303.03	71.56	1653.45
308.12	0.10	1293.20	308.16	0.10	1313.30	308.14	0.10	1330.57	303.04	73.60	1660.21
307.94	15.20	1373.96	308.19	15.21	1390.70	307.92	15.20	1408.48	303.15	74.79	1664.07
307.94	30.39	1442.79	308.17	30.40	1458.76	307.91	30.39	1475.46	303.09	75.99	1667.77
307.94	45.59	1505.03	308.18	45.60	1520.26	307.91	45.59	1535.97	308.04	0.10	1345.82^{a}
307.93	60.79	1561.90	308.18	60.79	1576.82	307.91	60.79	1592.39	308.09	15.20	1420.03
307.94	75.99	1615.55	308.17	76.02	1629.97	307.92	75.99	1644.67	307.97	30.39	1486.61
307.93	91.18	1664.79	308.12	91.20	16/9.20	307.92	91.18	1693.20	307.98	45.59	1546.89
307.94	101.32	1695.96	308.16	91.21	16/9.14	307.92	101.32	1/24.32	307.96	60.79	1603.08
313.09	0.10	12/0.31	308.12	101.32	1/10.26	313.11	0.10	1313.75	307.95	05.80	1620.93
312.91	15.20	1338.87	212.26	0.10	1290.40	212.91	15.20	1392.73	207.90	08.85	1631.20
312.90	30.39 45 59	1420.71	313.20	30.30	1373.07	312.91	30.39 45 59	1400.62	307.90	73.31	1646.24
312.90	60.79	15491.30	313.20	45 59	1506.12	312.91	45.59	1578.03	307.94	73.31	1650.01
312.90	75.99	1603.13	313.20	60.79	1563.47	312.91	75.99	1631.98	307.93	75.99	1655.12
312.90	91.18	1653.05	313.23	76.00	1616 59	312.91	91.18	1681.12	313.01	0.10	1329.03^{a}
312.91	101.32	1684 72	313.22	91.20	1666.84	312.91	101.32	1712.28	313.06	15 20	1404 47
318.37	0.10	1258.57	313.22	101.34	1697.76	318.29	0.10	1296.33	313.03	30.39	1471.90
318.30	15.20	1342.76	318.33	0.10	1279.15	318.39	15.20	1375.92	313.01	45.59	1532.53
318.29	30.39	1413.60	318.83	15.20	1357.83	318.39	30.39	1444.81	313.00	60.79	1589.39
318.29	45.59	1477.46	318.84	30.39	1427.84	318.39	45.59	1507.26	313.00	65.98	1607.83
318.29	60.79	1535.46	318.82	45.60	1491.03	318.38	45.59	1507.34	313.00	69.20	1618.90
318.29	75.99	1590.00	318.82	60.79	1549.17	318.38	60.79	1564.64	313.03	72.90	1631.48
318.29	91.18	1640.62	318.82	75.99	1603.39	318.38	75.99	1618.27	313.04	75.99	1641.73
318.29	101.32	1672.37	318.83	91.18	1653.69	318.39	91.18	1667.79	318.18	0.10	1311.69 ^a
			318.82	101.33	1684.88	318.38	91.18	1667.82	318.36	15.20	1387.67
						318.38	101.32	1699.14	318.44	30.39	1455.97
									318.45	30.39	1455.89
									318.44	45.59	1517.70
									318.41	60.79	1575.13
									318.40	65.95	1593.73
									518.45	12.00	1617.01
									318.43 318.42	/3.8/	1628.22
									J10.4J	13.77	1020.22

^a Published in a previous work.²²

less than $3 \cdot 10^{-7}$ for heptan-1-ol and octan-1-ol. Each sample was degassed in an ultrasonic cleaner just before the measurement. The purity of these chemicals was tested by comparing the densities and speeds of sound with literature values (Table 1).

Ultrasonic Speed Measurements. The speed of sound in liquids under test has been measured at atmospheric and higher pressures using two measuring sets designed and constructed in our laboratory. Two measuring vessels of the same acoustic path and construction have been used: one of them destined for measurements under atmospheric pressure, the other one for measurements under elevated pressures. A single transmitting—receiving ceramic transducer operating at 2 MHz and an acoustic mirror have been applied. The measuring sets operate on the principle of the pulse—echo—overlap method. The pressure was provided by a hand-operated hydraulic press and was measured with a strain gauge measuring system (Hottinger Baldwin System P3MD) with accuracy better than 0.15 %. The temperature was measured using an Ertco Hart 850 platinum

resistance thermometer (NIST certified) with an uncertainty of \pm 0.05 K and resolution of 0.001 K. All temperatures reported in this work are expressed in the International Temperature Scale of 1990 (ITS-90).

Re-distilled water, degassed by boiling just before measurements, was used as the standard liquid for determining the ultrasonic path length. The electrolytic conductivity of water was $1 \cdot 10^{-4}$ S·m⁻¹. The speed of sound in water under atmospheric pressure was calculated from the polynomial of Marczak,²³ while for higher pressures the equation of Kell and Whalley²⁴ was used. The uncertainty of the speed of sound measurements was estimated to be 0.03 % at atmospheric pressure, 0.04 % under pressures up to 60 MPa, and 0.05 % under pressures from (60 to 101) MPa. Other details of the highpressure device and the method of the speed of sound measurements can be found in a previous paper.²⁵

Density Measurements. The densities at atmospheric pressure were measured using a vibrating tube densimeter Anton Paar DMA 5000. The densimeter was calibrated with air and re-



Figure 1. Speed of sound in (a) heptan-1-ol, (b) octan-1-ol, (c) nonan-1-ol, and (d) decan-1-ol: \bullet , 293.15 K; \bigcirc , 298.15 K; \blacksquare , 303.15 K; \square , 308.15 K; \blacktriangle , 313.15 K; \triangle , 318.15 K. Lines calculated from empirical function: $u = \sum_{i=0}^{3} a_i p^i$.

distilled water of electrolytic conductivity as above and degassed by boiling just before the measurements. The uncertainty of the density measurements was 0.05 kg m⁻³, whereas the repeatability was estimated to be better than 0.005 kg m⁻³.

 Table 3. Densities of Alcohols Measured within the Temperature

 Range of (293 to 318) K at Atmospheric Pressure

hepta	un-1-ol	octan-1-ol		nonan-1-ol		daca	n-1-ol
<i>T</i> /K	$ ho/kg \cdot m^{-3}$	<i>T</i> /K	$ ho/kg \cdot m^{-3}$	<i>T</i> /K	$ ho/kg\cdot m^{-3}$	<i>T</i> /K	$ ho/kg\cdot m^{-3}$
293.151	822.297	293.151	825.048	293.155	827.660	293.150	829.758
298.150	818.796	298.148	821.636	298.155	824.239	298.150	826.370
303.152	815.269	303.151	818.173	303.156	820.800	303.150	822.950
308.150	811.724	308.149	814.675	308.155	817.345	308.150	819.570
313.152	808.158	313.149	811.171	313.153	813.868	313.150	816.120
318.151	804.546	318.149	807.654	318.150	810.376	318.150	812.634

Table 4. Coefficients of Polynomial (1) for the Speed of Sound and Density under Atmospheric Pressure within the Temperature Range of (293 to 318) K and Mean Deviations from the Regression Line

com- ponent	$c_0/{ m m}\cdot { m s}^{-1}$	$\begin{array}{c} c_{\mathrm{l}} / \\ \mathrm{m}^{\bullet} \mathrm{s}^{-1} \mathrm{\bullet} \\ \mathrm{K}^{-1} \end{array}$	$c_2 \cdot 10^{3/} \\ m \cdot s^{-1} \cdot \\ K^{-2}$	$\delta u_0/m \cdot s^{-1}$	$p_0/kg\cdot m^{-3}$	$\substack{\substack{\rho_l / \\ kg \boldsymbol{\cdot} m^{-3} \boldsymbol{\cdot} \\ K^{-1}}}_{K^{-1}}$	$\substack{ \rho_2 \cdot 10^4 / \\ kg \cdot m^{-3} \cdot \\ K^{-2} } $	$\delta ho/kg\cdot m^{-3}$
heptan -1-ol	2497.354	-4.416949	1.65176	0.04	983.002	-0.3993296	-5.07848	0.006
octan- 1-ol	2560.249	-4.714394	2.16735	0.02	983.294	-0.3955131	-4.92143	0.01
nonan- 1-ol	2555.809	-4.560609	1.89642	0.002	995.338	-0.4618601	-3.75632	0.001
decan- 1-ol	2696.695	-5.376703	3.21792	0.02	989.849	-0.4188373	-4.34218	0.02

Results

The ultrasonic speeds in heptan-1-ol, octan-1-ol, and nonan-1-ol have been measured from (293 to 318) K in about 5 K steps and under the pressures about (0.1, 15, 30, 45, 60, 75, 90, and 101) MPa. The ultrasonic speeds in decan-1-ol have been measured under the pressures about (0.1, 15, 30, 45, 60, and 76) MPa. The experimental values are listed in Table 2 and presented in Figure 1. The densities for the alcohols under test were measured under atmospheric pressure within the same temperature range. The experimental values are collected in Table 3.

The dependencies of the speed of sound and density on temperature at atmospheric pressure were approximated by second-order polynomials of the type:

$$y = \sum_{j=0}^{2} b_j T^j \tag{1}$$

where y is the speed of sound (u_0) or density (ρ) at atmospheric pressure (p_0) ; b_j are the polynomial coefficients $(b_j = c_j$ for the speed of sound, and $b_j = \rho_j$ for the density) calculated by the least-squares method. The backward stepwise rejection procedure was used to reduce the number of non-zero coefficients. The coefficients and the mean deviations from the regression lines are given in Table 4.

Since the sensitivity of the pressure gauge is lower than that of both the ultrasonic measuring set and the thermometer, the equation suggested by Sun et al.²⁶ was chosen in this work for smoothing out the speed of sound, pressure, and temperature:

$$p - p_0 = \sum_{i=1}^{m} \sum_{j=0}^{n} a_{ij} (u - u_0)^i T^j$$
(2)

where a_{ij} are the polynomial coefficients calculated by the leastsquares method, u is the speed of sound at p > 0.1 MPa, and u_0 is the speed calculated from eq 1. The coefficients a_{ij} and the mean deviations from the regression lines are given in Table 5. The stepwise rejection procedure was used to reduce the number of the non-zero coefficients.

The speeds of sound in octan-1-ol reported in this work are compared with those reported by Plantier et al.⁴ The absolute average deviation $(AAD = (100/n)\sum_{i=1}^{n} |u_{\text{lit},i}/u_{\text{exp},i} - 1|)$ was

Table 5. Coefficients of Equation 2 and Mean Deviations from the Regression Line δu

		K wirds in	m•s 1
61233304 147105•10 ⁻⁴	2.06383455•10 ⁻⁴		0.31
		$-2.76888747 \cdot 10^{-13}$	
803665851 835117•10 ⁻⁶	$3.16738349 \cdot 10^{-4}$ -4.20983029 \cdot 10^{-7}		0.28
23007509 $123867 \cdot 10^{-6}$	3.19513200•10 ⁻⁴ -4.18349839•10 ⁻⁷		0.31
94264772	$3.33303397 \cdot 10^{-4}$		0.25
	261233304 1147105·10 ⁻⁴ 203665851 23007509 2123867·10 ⁻⁶ 294264772 555104·10 ⁻⁷	$\begin{array}{r} 2.06383455 \cdot 10^{-4} \\ 2.06383455 \cdot 10^{-4} \\ 3.16738349 \cdot 10^{-4} \\ -4.20983029 \cdot 10^{-7} \\ 3.19513200 \cdot 10^{-7} \\ -4.18349839 \cdot 10^{-7} \\ 3.1923867 \cdot 10^{-6} \\ 3.3303397 \cdot 10^{-4} \\ 555104 \cdot 10^{-7} \\ -1.58502851 \cdot 10^{-9} \end{array}$	$\begin{array}{r} 2.06383455 \cdot 10^{-4} \\ -2.76888747 \cdot 10^{-13} \\ -2.76888747 \cdot 10^{-13} \\ -3.03665851 \\ 3.16738349 \cdot 10^{-4} \\ -4.20983029 \cdot 10^{-7} \\ -4.20983029 \cdot 10^{-7} \\ -3.3307509 \\ 3.19513200 \cdot 10^{-4} \\ -4.18349839 \cdot 10^{-7} \\ -3.123867 \cdot 10^{-6} \\ -3.33303397 \cdot 10^{-4} \\ 555104 \cdot 10^{-7} \\ -1.58502851 \cdot 10^{-9} \end{array}$

Table 6. Calculated Densities of Alcohols at Pressures up to 100 MPa and within the Temperature Limits of (293 and 318) K

			$\rho/\text{kg}\cdot\text{m}^{-3}$			
р			T/	K		
MPa	293.15	298.15	303.15	308.15	313.15	318.15
			Heptan-1-ol	l		
0.1^{a}	822.30	818.80	\$15.27	811.73	808.15	804.55
10	828.43	825.08	821.71	818.32	814.91	811.47
20	834.20	830.97	827.73	824.47	821.2	817.90
30	839.60	836.48	833.36	830.21	827.05	823.88
40	844.69	841.68	838.65	835.60	832.54	829.47
50	849.52	846.59	843.65	840.70	837.73	834.75
60	854.11	851.26	848.40	845.53	842.64	839.74
70	858.50	855.72	852.93	850.13	847.32	844.49
80	862.70	859.99	857.27	854.53	851.79	849.03
90	866.73	864.08	861.42	858.75	856.07	853.37
100	870.61	868.02	865.42	862.80	860.18	857.54
			Octan-1-ol			
0.1^{a}	825.06	821.62	818.17	814.68	811.18	807.65
10	831.02	827.73	824.42	821.08	817.73	814.36
20	836.63	833.46	830.28	827.07	823.85	820.62
30	841.90	838.84	835.76	832.67	829.56	826.44
40	846.87	843.91	840.93	837.94	834.93	831.91
50	851.59	848.71	845.82	842.91	840.00	837.07
60	856.08	853.28	850.47	847.64	844.81	841.96
70	860.38	857.65	854.90	852.15	849.39	846.61
80	864.49	861.83	859.15	856.46	853.76	851.05
90	868.44	865.84	863.22	860.60	857.96	855.31
100	872.25	869.70	867.14	864.57	861.99	859.40
			Nonan-1-ol			
0.1^{a}	827.66	824.24	820.80	817.35	813.87	810.38
10	833.48	830.20	826.91	823.59	820.27	816.92
20	838.97	835.81	832.64	829.45	826.25	823.04
30	844.12	841.07	838.01	834.93	831.84	828.74
40	849.00	846.04	843.07	840.09	837.10	834.09
50	853.62	850.75	847.87	844.97	842.07	839.15
60	858.03	855.23	852.43	849.62	846.79	843.95
70	862.24	859.52	856.79	854.05	851.29	848.53
80	866.28	863.63	860.96	858.29	855.60	852.90
90	870.16	867.57	864.97	862.35	859.73	857.09
100	873.91	871.37	868.82	866.27	863.70	861.11
			Decan-1-ol			
0.1^{a}	829.75	826.37	822.97	819.55	816.11	812.64
10	835.44	832.20	828.94	825.66	822.37	819.05
20	840.81	837.69	834.56	831.40	828.24	825.05
30	845.86	842.85	839.82	836.78	833.73	830.66
40	850.64	847.72	844.79	841.85	838.90	835.93
50	855.17	852.35	849.51	846.65	843.79	840.91
60	859.50	856.75	853.99	851.22	848.44	845.64
70		860.97	858.28	855.58	852.87	850.14

^{*a*} Calculated from eq 1.

found to be 0.06 %, which does not exceed the uncertainty of 0.2 % reported by them. A comparison of the speeds of sound in heptan-1-ol, octan-1-ol, nonan-1-ol, and decan-1-ol at 303.15 K obtained in this experiment for the whole pressure range with calculated by the correlation equation proposed by Khasanshin⁴ resulted in AAD values of 0.04 %, 0.03 %, 0.06 %, and 0.04 %, respectively.

Density, Isobaric Heat Capacity, and Derived Thermodynamic Properties under Elevated Pressures. The densities and

Table 7. Calculated Isobaric Molar Heat Capacities of Alcohols at Pressures up to 100 MPa and within the Temperature Limits of (293 and 318) K

		($C_p/J \cdot mol^{-1}K^{-1}$	-1		
р			T/	К		
MPa	293.15	298.15	303.15	308.15	313.15	318.15
			Heptan-1-ol			
0.1^{a}	268.13	272.98	278.01	283.17	288.44	293.77
10	267.10	271.94	276.92	282.03	287.26	292.57
20	266.20	271.02	275.97	281.04	286.22	291.52
30	265.40	270.20	275.12	280.16	285.31	290.58
40	264.67	269.45	274.35	279.36	284.49	289.73
50	264.01	268.77	273.64	278.03	283.73	288.96
60 70	263.39	268.13	272.98	277.95	283.04	288.24
/0	262.81	267.34	272.57	212.31	282.39	287.57
80	262.27	200.98	271.79	276.15	281.77	280.93
100	201.75	265.03	271.23	275.62	280.63	280.34
100	201.20	205.95	270.72	275.02	280.05	265.70
0.1a	207.51	202 47	Octan-1-ol	215 55	221 64	227 72
10	297.51	303.47	309.49	214.22	321.04	321.12
20	290.41	201.25	306.32	212.26	320.57	225 20
20	293.43	301.33	307.29	313.20	319.27	323.50
40	294.39	200.47	305.55	311.77	317.41	324.29
50	293.11	299.07	304.80	310.69	316.61	322.56
60	292.45	298.26	304.00	309.97	315.87	321.79
70	291.84	297.63	303.45	309.30	315.17	321.08
80	291.25	297.03	302.83	308.66	314 52	320.40
90	290.70	296.45	302.24	308.05	313.89	319.76
100	290.16	295.90	301.67	307.47	313.29	319.14
			Nonan-1-ol			
0.1^{a}	332.80	337 57	342.85	348 57	354 65	361.04
10	331.70	336.49	341.72	347.36	353.40	359.79
20	330.74	335.52	340.71	346 31	352.30	358.68
30	329.88	334 64	339.80	345 36	351 32	357.68
40	329.10	333.84	338.97	344.50	350.43	356.77
50	328.37	333.09	338.19	343.70	349.61	355.92
60	327.68	332.38	337.46	342.95	348.83	355.12
70	327.03	331.70	336.77	342.23	348.09	354.36
80	326.40	331.06	336.10	341.54	347.38	353.63
90	325.79	330.43	335.45	340.87	346.70	352.92
100	325.19	329.81	334.82	340.22	346.03	352.24
			Decan-1-ol			
0.1^{b}	367.12	372.61	378.31	378.31	390.31	396.62
10	365.90	371.34	376.99	382.85	388.90	395.17
20	364.80	370.21	375.83	381.64	387.66	393.88
30	363.82	369.20	374.78	380.56	386.54	392.73
40	362.93	368.28	373.83	379.58	385.53	391.68
50	362.10	367.42	372.94	378.67	384.59	390.71
60	361.32	366.62	372.11	377.81	383.71	389.81
70		365.85	371.33	371.33	382.87	388.94

^a Values from ref 29. ^b Values from ref 22.

isobaric heat capacities of heptan-1-ol, octan-1-ol, nonan-1-ol, and decan-1-ol were determined for temperatures from (293 to 318) K and for pressures up to 100 MPa for the first three alkanols and up to 70 MPa for the latter one. Details of the algorithm were discussed in previous works.^{27,28} In the calculations, the experimental speeds of sound under elevated pressures have been used, together with the densities and heat capacities at atmospheric pressure. The temperature dependence of the isobaric heat capacity was taken from the literature. The polynomials reported by Zábranský et al.29 were used for heptan-1-ol, octan-1-ol, and nonan-1ol, while for decan-1-ol the polynomial reported by Dzida and Góralski²² was applied. The calculated density and isobaric heat capacity values are listed in Tables 6 and 7, respectively. The uncertainty of the measured speeds of sound cause a maximum error of 0.02 % in the densities calculated for elevated pressures. The quality of the densities, obtained in this work, was checked by comparisons: (a) with the densities of octan-1-ol and decan-1-ol measured by Matsuo and Makita¹⁸ by means of a vibrating densimeter at 298.15 K and pressures up to 40 MPa (the AAD values were found to be 0.07 % and 0.05 % for octan-1-ol and decan-1-ol, respectively, at atmospheric pressure as well as higher pres-

Table 8.	Isentropic Compressibilities of Alcohols at Pressures up	to to
100 MPa	and within the Temperature Limits of (293 and 318) K	

			$\kappa_{S} \cdot 10^{9} / Pa^{-1}$						
р	р Т/К								
MPa	293.15	298.15	303.15	308.15	313.15	318.15			
			Heptan-1-o	1					
0.1	0.6728	0.6933	0.7146	0.7367	0.7598	0.7838			
10	0.6201	0.6373	0.6551	0.6734	0.6924	0.7120			
20	0.5767	0.5915	0.6067	0.6224	0.6384	0.6550			
30	0.5403	0.5533	0.5666	0.5802	0.5941	0.6084			
40	0.5092	0.5207	0.5325	0.5445	0.5567	0.5693			
50	0.4821	0.4924	0.5029	0.5137	0.5246	0.5358			
60	0.4582	0.4675	0.4770	0.4867	0.4966	0.5066			
70	0.4369	0.4454	0.4541	0.4629	0.4718	0.4809			
80	0.4177	0.4256	0.4335	0.4416	0.4497	0.4580			
90	0.4004	0.4077	0.4150	0.4224	0.4298	0.4374			
100	0.3847	0.3914	0.3981	0.4049	0.4118	0.4188			
			Octan-1-ol						
0.1	0.6510	0.6705	0.6907	0.7117	0.7334	0.7560			
10	0.6018	0.6185	0.6357	0.6534	0.6717	0.6905			
20	0 5609	0 5754	0 5902	0.6055	0.6212	0.6373			
30	0 5263	0 5391	0.5522	0.5655	0 5792	0.5932			
40	0.4965	0.5079	0.5196	0.5315	0.5436	0.5559			
50	0.4706	0.4809	0.4913	0.5020	0.5128	0.5237			
60	0 4477	0 4570	0 4665	0 4761	0.4858	0 4956			
70	0.4272	0 4358	0 4444	0.4531	0.4619	0 4709			
80	0.4089	0 4167	0 4246	0.4326	0 4407	0 4488			
90	0 3923	0 3995	0.4068	0 4141	0.4215	0 4289			
100	0.3771	0.3838	0.3906	0.3973	0.4041	0.4110			
			Nonan-1-ol						
0.1	0.6328	0.6515	0.6709	0.6911	0.7120	0 7338			
10	0.5860	0.6020	0.6186	0.6357	0.6534	0.7558			
20	0.5469	0.5609	0.5753	0.5901	0.6053	0.6200			
30	0.5138	0.5007	0.5389	0.5510	0.5652	0.0209			
40	0.4853	0.3202	0.5557	0.5103	0.5052	0.5788			
50	0.4604	0.4704	0.4806	0.4910	0.5016	0.5451			
60	0.4384	0.4475	0.4568	0.4661	0.4757	0.4853			
70	0.4188	0.4271	0.4355	0.4441	0.4527	0.4615			
80	0.4011	0.4271	0.4165	0.4243	0.4322	0.4013			
00	0.3851	0.3021	0.3003	0.4065	0.4138	0.4402			
100	0.3705	0.3770	0.3836	0.3903	0.3970	0.4038			
100	0.5705	0.5770	0.5050	0.5705	0.3770	0.4050			
0.1	0 (175	0.6257	Decan-1-ol	0 (741	0 (0.42	0.7151			
0.1	0.61/5	0.6357	0.6546	0.6/41	0.6942	0./151			
10	0.5732	0.5890	0.6053	0.6221	0.6394	0.6571			
20	0.5359	0.5498	0.5640	0.5787	0.5936	0.6090			
30	0.5041	0.5165	0.5291	0.5420	0.5552	0.5686			
40	0.4766	0.4877	0.4990	0.5105	0.5222	0.5341			
50	0.4525	0.4626	0.4728	0.4831	0.4936	0.5042			
60	0.4312	0.4404	0.4496	0.4590	0.4684	0.4780			
70		0.4205	0.4290	0.4375	0.4461	0.4547			

sures); (b) with densities calculated from the speeds of sound reported by Plantier et al.⁴ for octan-1-ol at (303.15 and 313.15) K and pressures up to 50 MPa (the AAD values are 0.07 % and 0.06 % for (303.15 and 313.15) K, respectively, at atmospheric and higher pressures), and (c) with densities calculated by Khasanshin,30 who published correlation equations between the density and the number of carbon atoms ranging from 4 to 10 for pressures up to 50 MPa at (293.15 and 298.15) K (the AAD values are 0.04 %, 0.04 %, 0.02 %, and 0.05 % for heptan-1-ol, octan-1-ol, nonan-1ol, and decan-1-ol, respectively). The above discrepancies are of order of uncertainty declared by Matsuo and Makita¹⁸ (\pm 0.06 %) and Plantier et al.4 (0.1 %). The values of measured speeds of sound and calculated densities of the alcohols under test are generally in a very good agreement with the literature ones providing a high quality of the obtained thermodynamic properties determined. Unfortunately, the quality of the isobaric heat capacities obtained from the ultrasonic measurements is worse than that of the densities which results from the principles of the method.²⁸

From the densities and speeds of sound, the adiabatic compressibilities were calculated by the Laplace formula: $\kappa_S = (\rho u^2)^{-1}$. Results of the calculations are given in Table 8. The isothermal compressibility was calculated from the adiabatic one by the well-known relationship:

$$\kappa_T = \kappa_S + \frac{\alpha_p^2 V T}{C_p} \tag{3}$$

Table 9. Calculated Isobaric Thermal Expansion of Alcohols at
Pressures up to 100 MPa and within the Temperature Limits of
(293 and 318) K

			$\alpha_{p} \cdot 10^{3}/\text{K}^{-1}$	1		
р			T/	K		
MPa	293.15	298.15	303.15	308.15	313.15	318.15
			Heptan-1-o	1		
0.1	0.8477	0.8575	0.8675	0.8775	0.8877	0.8980
10	0.8061	0.8145	0.8230	0.8315	0.8402	0.8489
20	0.7704	0.7777	0.7852	0.7927	0.8003	0.8079
30	0.7393	0.7459	0.7526	0.7526	0.7662	0.7731
40	0.7119	0.7180	0.7241	0.7302	0.7365	0.7427
50	0.6875	0.6931	0.6987	0.7044	0.7102	0.7160
60	0.6654	0.6706	0.6759	0.6759	0.6867	0.6921
70	0.6453	0.6503	0.6553	0.6603	0.6654	0.6706
80	0.6269	0.6316	0.6364	0.6412	0.6461	0.6510
90	0.6099	0.6145	0.6191	0.6237	0.6284	0.6331
100	0.5942	0.5986	0.6031	0.6076	0.6121	0.6167
			Octan-1-ol			
0.1	0.8291	0.8386	0.8481	0.8578	0.8676	0.8774
10	0.7896	0.7977	0.8058	0.8141	0.8224	0.8308
20	0.7552	0.7623	0.7694	0.7767	0.7839	0.7913
30	0.7252	0.7315	0.7379	0.7443	0.7508	0.7574
40	0.6985	0.7043	0.7101	0.7159	0.7219	0.7278
50	0.6746	0.6799	0.6853	0.6907	0.6962	0.7017
60	0.6530	0.6580	0.6630	0.6681	0.6732	0.6784
70	0.6333	0.6380	0.6428	0.6476	0.6525	0.6574
80	0.6152	0.6198	0.6243	0.6290	0.6336	0.6383
90	0.5985	0.6029	0.6074	0.6119	0.6164	0.6209
100	0.5831	0.5874	0.5917	0.5961	0.6005	0.6049
			Nonan-1-ol	1		
0.1	0.8241	0.8321	0.8402	0.8483	0.8565	0.8649
10	0.7854	0.7923	0.7992	0.8063	0.8134	0.8205
20	0.7516	0.7577	0.7639	0.7701	0.7764	0.7827
30	0.7218	0.7274	0.7330	0.7386	0.7444	0.7501
40	0.6953	0.7004	0.7057	0.7109	0.7162	0.7216
50	0.6714	0.6763	0.6812	0.6862	0.6912	0.6962
60	0.6496	0.6543	0.6591	0.6638	0.6687	0.6735
70	0.6297	0.6343	0.6389	0.6435	0.6482	0.6529
80	0.6114	0.6159	0.6204	0.6250	0.6296	0.6342
90	0 5944	0 5989	0.6033	0.6079	0.6124	0.6170
100	0.5786	0.5830	0.5875	0.5920	0.5965	0.6011
			Decan-1-ol			
0.1	0.8116	0.8303	0.8288	0.8376	0.8464	0.8554
10	0.7735	0.7810	0.7885	0.7962	0.8038	0.8116
20	0.7400	0.7466	0.7533	0.7601	0.7669	0.7739
30	0.7103	0.7163	0.7224	0.7286	0.7348	0.7411
40	0.6838	0.6894	0.6950	0.7007	0.7065	0.7123
50	0.6598	0.6651	0.6705	0.6758	0.6813	0.6867
60	0.6381	0.6431	0.6482	0.6534	0.6585	0.6638
70		0.6230	0.6280	0.6329	0.6380	0.6430

where α_p is the isobaric thermal expansion calculated from definition: $\alpha_p = -(1/\rho)(\partial \rho/\partial T)_p$. The values of the isobaric thermal expansion and the isothermal compressibility are listed in Tables 9 and 10, respectively.

The exact thermodynamic isothermal volume dependence of internal energy (i.e., the internal pressure) was derived from the basic thermodynamic relation dU = T dS - p dV as follows:

$$p_{\text{int}} \equiv \left(\frac{\partial U}{\partial V}\right)_T = T\left(\frac{\partial S}{\partial V}\right)_T - p = T\left(\frac{\partial p}{\partial T}\right)_V - p \tag{4}$$

where $(\partial p/\partial T)_V$ is the thermal pressure coefficient. Equation 4 can be rewritten in the following form:

$$p = T \left(\frac{\partial p}{\partial T}\right)_V - \left(\frac{\partial U}{\partial V}\right)_T \tag{5}$$

Thus, two definitions of the internal pressure can be found in the literature: one as given by eq 4^{31-43} or multiplied by $-1.^{44-48}$ The total pressure of the system consists of two parts. The first term on the right-hand side represents the kinetic pressure due to the thermal motion. The second one is the static pressure called the internal pressure due to intermolecular energy. The latter can be positive, negative, or, as in the case of ideal gas, zero.

Table 10. Isothermal Compressibilities of Alcohols at Pressures up to 100 MPa and within the Temperature Limits of (293 and 318) K 109/Po-1

			<i>k</i> _T 10 /1 a						
р	T/K								
MPa	293.15	298.15	303.15	308.15	313.15	318.15			
			Heptan-1-0	1					
0.1	0 7838	0.8073	0.8316	0.8567	0.8828	0 9099			
10	0.7202	0.7398	0.7599	0.7807	0.8021	0.8242			
20	0.6678	0.6846	0.7018	0.7195	0.7376	0.7562			
30	0.6239	0.6386	0.6536	0.6690	0.6847	0.7007			
40	0.5864	0.5994	0.6127	0.6263	0.6401	0.6541			
50	0.5538	0.5655	0.5774	0.5895	0.6018	0.6143			
60	0.5252	0.5358	0.5465	0.5574	0.5685	0.5797			
70	0.4997	0.5094	0.5192	0.5291	0.5392	0.5493			
80	0.4769	0.4858	0.4947	0.5038	0.5130	0.5223			
90	0.4563	0.4645	0.4727	0.4811	0.4895	0.4981			
100	0.4375	0.4451	0.4528	0.4605	0.4683	0.4762			
			Octan-1-ol						
0.1	0.7579	0.7800	0.8028	0.8265	0.8511	0.8765			
10	0.6985	0.7172	0.7365	0.7564	0.7770	0.7981			
20	0.6490	0.6652	0.6818	0.6990	0.7165	0.7345			
30	0.6072	0.6215	0.6361	0.6510	0.6663	0.6819			
40	0.5714	0.5841	0.5971	0.6103	0.6237	0.6375			
50	0.5402	0.5516	0.5632	0.5751	0.5871	0.5993			
60	0.5127	0.5231	0.5336	0.5443	0.5551	0.5660			
70	0.4882	0.4977	0.5073	0.5170	0.5268	0.5367			
80	0.4663	0.4750	0.4838	0.4927	0.5016	0.5107			
90	0.4464	0.4545	0.4626	0.4708	0.4790	0.4873			
100	0.4284	0.4359	0.4434	0.4510	0.4586	0.4662			
			Nonan-1-o	1					
0.1	0.7370	0.7585	0.7806	0.8034	0.8269	0.8511			
10	0.6803	0.6987	0.7175	0.7367	0.7565	0.7767			
20	0.6330	0.6489	0.6652	0.6819	0.6988	0.7161			
30	0.5929	0.6071	0.6214	0.6360	0.6508	0.6659			
40	0.5585	0.5711	0.5839	0.5969	0.6101	0.6234			
50	0.5284	0.5398	0.5514	0.5631	0.5749	0.5868			
60	0.5019	0.5123	0.5228	0.5334	0.5441	0.5548			
70	0.4782	0.4878	0.4974	0.5071	0.5168	0.5266			
80	0.4570	0.4658	0.4747	0.4836	0.4925	0.5014			
90	0.4378	0.4459	0.4542	0.4624	0.4706	0.4788			
100	0.4203	0.4279	0.4355	0.4432	0.4508	0.4584			
			Decan-1-o	l					
0.1	0.7178	0.7388	0.7605	0.7827	0.8057	0.8294			
10	0.6640	0.6822	0.7008	0.7199	0.7395	0.7596			
20	0.6187	0.6346	0.6509	0.6674	0.6844	0.7018			
30	0.5802	0.5943	0.6087	0.6232	0.6382	0.6534			
40	0.5469	0.5595	0.5724	0.5854	0.5987	0.6121			
50	0.5178	0.5292	0.5408	0.5525	0.5645	0.5765			
60	0.4921	0.5025	0.5130	0.5236	0.5344	0.5453			
70		0.4787	0.4884	0.4980	0.5079	0.5177			

Table 11. Internal Pressure of Alcohols at Pressures up to 100 MPa and within the Temperature Limits of (293 and 318) K $p_{\text{int}} \cdot 10^{-6} / \text{Pa}$

303.15

Heptan-1-ol

316.2

318.3

319.2

319.1

318.2

316.8

314.9

312.6

310.0

307.0

303.8

Octan-1-ol

320.1

321.7

322.1

321.7

320.5

318.9

316.7

314.1

311.2

308.0

304.5

Nonan-1-ol

326.2

327.7

328.1

327.6

326.3

324.5

322.2

3194

316.2

312.7

308.9

Decan-1-ol

330.3

331.1

330.8

329.7

328.0

325.6

р MPa

0.1

10

20

30

40

50

60

70

80

90

100

0.1

10

20

30

40

50

60

70

80

90

100

0.1

10

20

30

40

50

60

70

80

90

100

0.1

10

20

30

40

50

60

293.15

317.0

318.1

318.2

317.4

315.9

313.9

311.4

308.5

305.3

301.8

298.1

320.6

321.4

321.2

320.1

318.4

316.1

313.4

310.3

306.8

303.0

299.0

327.7

328.4

328.1

326.9

325.0

322.5

319.5

316.0

312.2

308.0

303.6

331.3

331.5

330.6

328.8

326.4

323.4

320.0

298.15

316.6

318.3

318.7

318.3

317.1

315.4

313.2

310.6

307.7

304.4

301.0

320.4

321.6

321.7

320.9

319.5

317.5

315.1

312.2

309.0

305.5

301.8

327.0

328.1

328.1

327.2

325.7

323.5

320.8

3177

314.2

310.4

306.2

330.9

331.3

330.7

329.3

327.2

324.6

T/K

308.15

315.5

318.2

319.5

319.8

319.3

318.2

316.6

314.6

312.2

309 5

306.6

3197

321.6

322.4

322.3

321.5

320.1

318.3

316.0

313.4

310.5

307.3

325.3

327.2

328.0

327.9

327.0

325.5

323.5

321.1

318.3

3151

311.6

329.6

330.8

330.9

330.1

328.7

326.7

313.15

314.8

318.0

319.8

320.4

320.3

319.5

318.2

316.5

314.4

312.0

309.3

3191

321.5

322.6

322.9

322.4

321.4

319.8

317.9

315.6

312.9

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326.7

327.9

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328.0 329.9

330.7

330.7

330.0

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322.8 321.4 324.2 325.6 327.0 70 317.9 319.6 321.4 323.1 324.9 the volume with temperature becomes lower with increasing pressure due to stronger hydrogen bonds caused by the σ -bond cooperativity. The increase in the association with increasing pressure is indicated also by the decreasing of isobaric heat capacities. Because of the relation between the isobaric heat capacity and entropy $(C_p = T(\partial S/\partial T)_p)$, the isobaric heat capacity is an approximated indicator of the molecular structure. Association of alcohol molecules provides an increase of the molecular order. Moreover the isothermal compression of liquid reduces the free volume and the amplitude of molecular vibrations. The effect of pressure on the volume was found to increase with increasing temperature, which is related doubtless to the increasing number of broken hydrogen bonds that makes the system more elastic. However the volume change due to the formation of hydrogen bonds is not too large as compared to the molar volume. This suggests that probably the nonspecific interactions and structural contributions, connected with the change of intermolecular distances in the compressed liquid, play also important role.

Moreover with increasing pressure, the influence of pressure on the temperature dependence of isobaric thermal expansion and isothermal compressibility decreasing. It demonstrates the existence a possible crossing point of isotherms at higher pressures. The crossing point of isobaric thermal expansion is characteristic for simple liquids; for isothermal compressibility

The thermal pressure coefficient and thereby the internal pressure are related to the isothermal compressibility and isobaric thermal expansion in the following way:

$$p_{\rm int} = \frac{T\alpha_p}{\kappa_T} - p \tag{6}$$

Therefore the internal pressures have been calculated using the corresponding κ_T and α_p values. The values of the internal pressures of the alcohols under test are collected in Table 11. The uncertainty of internal pressures obtained in this work is estimated to be better than ± 1 %.

The results of the calculations are shown in Figures 2 to 6. For clarity the lines and points are presented.

The densities of all the alcohols increase monotonically with increasing pressure and decreasing temperature (Figure 2). The isobaric heat capacity decreases with increasing pressure and increases with increasing temperature; however, the effect of pressure on this quantity is rather small in comparison with that of temperature. The effects of pressure and temperature on the isobaric heat capacity of the alcohols under test are shown in Figure 3. The isobaric thermal expansion and isothermal compressibility depend significantly on pressure in the vicinity of the atmospheric pressure, while with increasing pressure the effect gradually decreases (Figures 4 and 5). The increase of





Figure 2. Densities of (a) heptan-1-ol, (b) octan-1-ol, (c) nonan-1-ol, and (d) decan-1-ol: •, 293.15 K; \bigcirc , 298.15 K; \blacksquare , 303.15 K; \square , 308.15 K; \blacktriangle , 313.15 K; \triangle , 318.15 K. Lines calculated from empirical function: $\rho = \sum_{i=0}^{3} a_i p^i$.

this effect was not observed.^{49,50} Randzio et al.⁵⁰ suggested the correlation between the pressure of the crossing point of α_p and the nature of liquids. For example the isotherms of α_p of hexane cross each other at 65 ± 2 MPa.⁴⁹ For associated liquids a shift of the crossing points toward the higher pressure region was

Figure 3. Isobaric molar heat capacities of (a) heptan-1-ol, (b) octan-1-ol, (c) nonan-1-ol, and (d) decan-1-ol: \bullet , 293.15 K; \bigcirc , 298.15 K; \blacksquare , 303.15 K; \square , 308.15 K; \square , 308.15 K; \triangle , 313.15 K; \triangle , 318.15 K. Lines calculated from empirical function: $C_p = \sum_{i=0}^{3} a_i p^i$.

observed. For example for hexan-1-ol, the crossing point appears in the vicinity of 280 MPa; however, for water the crossing point is observed close to 450 MPa.⁵⁰ Therefore, the determination of the isobaric thermal expansion of the alcohols under



Figure 4. Isobaric thermal expansion of (a) heptan-1-ol, (b) octan-1-ol, (c) nonan-1-ol, and (d) decan-1-ol: \bullet , 293.15 K; \bigcirc , 298.15 K; \blacksquare , 303.15 K; \square , 308.15 K; △, 313.15 K; △, 318.15 K. Lines calculated from empirical function: $\alpha_p = \sum_{i=0}^{3} a_i p^i$.

test in the wider temperature and pressure ranges seems to be of interest.

Molecular interactions related to the work of intermolecular forces that accompanying the volume change are also manifested



Figure 5. Isothermal compressibity of (a) heptan-1-ol, (b) octan-1-ol, (c) nonan-1-ol, and (d) decan-1-ol: \bullet , 293.15 K; \bigcirc , 298.15 K; \blacksquare , 303.15 K; \square , 308.15 K; \triangle , 313.15 K; \triangle , 318.15 K. Lines calculated from empirical function: $\kappa_T = \sum_{i=0}^{3} a_i p^i$.

in the internal pressure.⁵¹ The internal pressure of liquids is a sum of the repulsion and attraction forces between molecules of the liquid.^{35,36,39} Since $(\partial p/\partial T)_V = (\partial S/\partial V)_T$, the internal



Figure 6. Internal pressure of (a) heptan-1-ol, (b) octan-1-ol, (c) nonan-1-ol, and (d) decan-1-ol: \bullet , 293.15 K; \bigcirc , 298.15 K; \blacksquare , 303.15 K; \square , 308.15 K; \blacktriangle , 313.15 K; \triangle , 318.15 K. Lines calculated from empirical function: $p_{int} = \sum_{i=0}^{3} a_i p^i$.

pressure is related to the isothermal change of entropy per unit volume and can be discussed in terms of order in liquids resulting from isothermal expansion. A very interesting pressure and temperature dependence of the internal pressure of the alcohols under test was observed (Figure 6). A crossing point of the isotherms exists for all of the alcohols studied. The pressure of the crossing point is characteristic for each alcohol and is observed at rather low pressures up to 22 MPa. The internal pressure decreases with increasing temperature at pressures up to the crossing point, and then it increases with the increase of temperature. Moreover, the internal pressure as a function of pressure shows a maximum (i.e., the internal pressure first increases with increasing pressure and then it decreases). With increasing temperature the maximum moves toward higher pressures. The existence of a maximum of the pressure dependence of the internal pressure was reported in the literature.^{41,52} Under low pressures, as the temperature is increasing, the repulsive part of the internal pressure becomes more predominant, but at constant temperature the resultant forces under low-pressure conditions are attractive. A change in the molar volume is always accompanied by a corresponding change in the mean molecular distance. As the pressure increases the repulsive forces become predominant. Thus at high pressures, the increasing temperature causes an increase of the internal pressure at high pressures. The internal pressure increases with pressure and decreases with temperature due to the shift of the thermodynamic equilibrium of association. However, the decrease of internal pressure with increasing pressure and the increase with increasing temperature suggest that the possible nonspecific interactions, connected with the variation of intermolecular distances in the compressed liquid, play also an important role. Kartsev et al.^{45–48} showed that the temperature coefficient of internal pressure is sensitive to the structural organization of the liquid and reflects the character of the interactions. According to the sign of the temperature coefficient of the internal pressure, liquids can be classified as not hydrogen-bonded or weakly associated and hydrogenbonded.48 Alcohols are characterized also by the inversion of the temperature dependence of the internal pressure.⁴⁵ For the alcohols under test, such an inversion is observed at temperatures higher than 318.15 K.45

However to the best of my knowledge, a reliable molecular theory of the internal pressure has not been worked out yet. Thus, I decided to postpone further discussion of the internal pressure until necessary data for liquids and liquid mixtures at elevated pressures are available.

Summary

The speeds of sound in heptan-1-ol, octan-1-ol, nonan-1-ol, and decan-1-ol have been measured at temperatures from (293to 318) K and at pressures up to 101 MPa for heptan-1-ol, octan-1-ol, and nonan-1-ol and up to 76 MPa for decan-1-ol. The densities of the liquids under test have been measured within the same temperature range under atmospheric pressure. From the measurement results, the pressure and temperature dependence of the density and isobaric heat capacity have been determined using the modified method of Davis and Gordon.⁸ This enables the determination of the isothermal and adiabatic compressibility, the isobaric thermal expansion, and the internal pressure as a function of temperature and pressure. A simple association model qualitatively explains the pressure and temperature dependence of the volumetric properties of alcohols. Interesting temperature and pressure dependences of the internal pressure of the alcohols under test have been observed.

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Literature Cited

- Cibulka, I.; Ziková, M. Liquid densities at elevated pressures of 1-alkanols from C₁ to C₁₀: a critical evaluation of experimental data. *J. Chem. Eng. Data* **1994**, *39*, 876–86.
- (2) Oakley, B. A.; Barber, G.; Worden, T.; Hanna, D. Ultrasonic parameters as a function of absolute hydrostatic pressure. I. A review of the data for organic liquids. *J. Phys. Chem. Ref. Data* **2003**, *32*, 1501–1533.
- (3) Khasanshin, T. S. Sonic velocity in liquid primary normal alcohols. *Teplofiz. Vys. Temp.* **1991**, *29*, 710–716.
- (4) Plantier, F.; Daridon, J. L.; Lagourette, B. Nonlinear parameter (B/A) measurements in methanol, 1-butanol and 1-octanol for different pressures and temperatures. J. Phys. D: Appl. Phys. 2002, 35, 1063–1067.
- (5) Marczak, W.; Dzida, M.; Ernst, S. Determination of the thermodynamic properties of 1-propanol and 1-hexanol from speed of sound measurements under elevated pressures. *High Temp.*-*High Pressures* 2000, *32*, 283–292.
- (6) Dzida, M.; Żak, A.; Ernst, S. Thermodynamic and acoustic properties of binary mixtures of alcohols and alkanes. I. Speed of sound in (ethanol + *n*-heptane) under elevated pressures. *J. Chem. Thermodyn.* 2005, 37, 405–414.
- (7) Dzida, M.; Marczak, W. Thermodynamic and acoustic properties of binary mixtures of alcohols and alkanes. II. Density and heat capacity of (ethanol + n-heptane) under elevated pressures. J. Chem. Thermodyn. 2005, 37, 826–836.
- (8) Davis, L. A.; Gordon, R. B. Compression of mercury at high pressure. *J. Chem. Phys.* **1967**, *46*, 2650–2660.
- (9) Sun, T. F.; Ten, Seldam, C. A.; Kortbeek, P. J.; Trappeniers, N. J.; Biswas, S. N. Acoustic and thermodynamic properties of ethanol from 273.15 to 333.15 K and up to 280 MPa. *Phys. Chem. Liq.* **1988**, *18*, 107–116.
- (10) Kulig, A. Wolumetryczne i akustyczne właściwości binarnych mieszanin alkanol-1,2-etanodiol. Diploma Thesis, 2004.
- (11) Aralaguppi, M. I.; Jadar, C. V.; Aminabhavi, T. M. Density, viscosity, refractive index, and speed of sound in binary mixtures of acrylonitrile with methanol, ethanol, propan-1-ol, butan-1-ol, pentan-1-ol, hexan-1-ol, heptan-1-ol, and butan-1-ol. *J. Chem. Eng. Data* **1999**, *44*, 216– 221.
- (12) Calvo, E.; Brocos, P.; Piñeiro, Á.; Pintos, M.; Amigo, A; Bravo, R.; Roux, A. H.; Roux-Desgranges, G. Heat capacities, excess enthalpies, and volumes of mixtures containing cyclic ethers. 4. Binary systems 1,4-dioxane + 1-alkanols. J. Chem. Eng. Data 1999, 44, 948–954.
- (13) Uosaki, Y.; Hamaguchi, T.; Moriyoshi, T. Excess molar volumes of (3-methyl-2-oxazolidinone+ an alkan-1-ol) at 298.15 K, 313.15 K, and 328.15 K. *Fluid Phase Equilib.* **1997**, *136*, 299–306.
- (14) Gepert, M.; Ernst, S. Interpretation of the excess molar volumes and excess molar compressions of pentan-1-ol + octan-1-ol mixtures on the basis of the homomorf concept. *J. Solution Chem.* **2003**, *32*, 831–852.
- (15) Kiyohara, O.; Benson, G. C. Ultrasonic speeds and isentropic compressibilities of n-alkanol + n-heptane mixtures at 298.15 K. J. Chem. Thermodyn. 1979, 11, 861–873.
- (16) Nath, J. Speeds of sound in and isentropic compressibilities of (n-octanol + n-hexane, or n-heptane, or n-octane) at T = 298.15 K. Fluid Phase Equilib. 2002, 203, 261–268.
- (17) Cibulka, I.; Heintz, A. Partial molar volumes of air-component gases in binary liquid mixtures with *n*-alkanes and 1-alkanols at 298.15 K. *Fluid Phase Equilib.* **1995**, *107*, 235–255.
- (18) Matsuo, S.; Makita, T. Volumetric properties of 1-alkanols at temperatures in the range 298–348 K and pressures up to 40 MPa. *Int. J. Thermophys.* **1989**, *10*, 885–897.
- (19) Lubowiecka, B., Wolumetryczne, akustyczne i wiskozymetryczne badania binarnych mieszanin etano-1,2-diol + nonan-1-ol. Diploma Thesis, University of Silesia, Katowice, Poland, 2003.
- (20) Stolińska, M., Badania akustycznych i termodynamicznych właściwości binarnych mieszanin propan-2-olu a alkanolami. Diploma Thesis, University of Silesia, Katowice, Poland, 2006.
- (21) Diaz, Pena, M.; Tardajos, G. Isothermal compressibilities of *n*-alcohols from methanol to 1-dodecanol at 298.15, 308.15, 318.15, and 333.15 K. J. Chem. Thermodyn. **1979**, 11, 441–445.
- (22) Dzida, M.; Góralski, P Excess molar heat capacities for (decan-1-ol + n-heptane) at temperatures from (290 to 318) K. Experimental results and theoretical description using the ERAS model. *J. Chem. Thermodyn.* **2006**, *38*, 962–969.
- (23) Marczak, W. Water as a standard in the measurements of speed of sound in liquids. J. Acoust. Soc. Am. 1997, 102, 2776–2779.
- (24) Kell, G. S.; Whalley, E. Reanalysis of the density of liquid water in the range 0–150 °C and 0–1 kbar. J. Chem. Phys. 1975, 62, 3496– 3503.

- (25) Dzida, M.; Chorążewski, M.; Zorêbski, M.; Mańka, R. Modifications of a high pressure device for speed of sound measurements in liquids. *J. Phys. IV* 2006, *137*, 203–207.
- (26) Sun, T.; Biswas, S. N.; Trappeniers, N. J.; Ten, Seldam, C. A. Acoustic and thermodynamic properties of methanol from 273 to 333 K and at pressures to 280 MPa. J. Chem. Eng. Data 1988, 33, 395–398.
- (27) Marczak, W.; Dzida, M.; Ernst, S. Determination of the thermodynamic properties of (1) -propanol and 1-hexanol from speed of sound measurements under elevated pressures. *High Temp.* –*High Pressures* 2000, *32*, 283–292.
- (28) Dzida, M. The effect of pressure on the thermodynamic properties of propan-1-ol + *n*-heptane mixtures. J. Solution Chem. 2004, 33, 527– 547.
- (29) Zábranský, M.; Růžička, V.; Domalski, E. S. Heat capacity of liquids: critical review and recommended values. Supplement I. J. Phys. Chem. Ref. Data 2002, 30, 1199–1689.
- (30) Khasanshin, T. S. "Structure-property" quantitative correlations for the density of primary normal alcohols. *Teplofiz. Vys. Temp.* 1997, 35, 886–895.
- (31) Hildebrand, J. H. Theory of solubility. Phys. Rev. 1923, 21, 46-52.
- (32) Westwater, W.; Frantz, H. W.; Hildebrand, J. H. Internal pressure of pure and mixed liquids. *Phys. Rev.* **1929**, *31*, 135–144.
- (33) Srivastava, S. C.; Berkowitz, N. On the relationship between internal pressure and ultrasonic velocity. *Can. J. Chem.* **1963**, *41*, 1787– 1793.
- (34) Bagley, E. B.; Nelson, T. P.; Scigliano, J. M. Internal pressure of liquids and their relationship to the enthalpies and entropies of mixing in nonelectrolite solutions. *J. Phys. Chem.* **1973**, *77*, 2794– 2798.
- (35) Lugo, L.; Comuñas, M. J. P.; López, E. R.; Fernández, J. (*p*, V_m, *T*, *x*) measurements of dimethyl carbonate + octane binary mixtures. I. Experimental results, isothermal compressibilities, isobaric expansivities and internal pressures. *Fluid Phase Equilib.* 2001, 186, 235–255.
- (36) Goharshadi, E. K.; Nazari, F. Computation of internal pressure of liquids using a statistical mechanical equation of state. *Fluid Phase Equilib.* 2001, 187–188, 425–431.
- (37) Marczak, W. Internal pressure of a thermodynamically ideal mixture and the excess internal pressure. *Phys. Chem. Chem. Phys.* 2002, 4, 1889–1890.
- (38) Pandey, J. D.; Sanguri, V.; Bhatt, B. D. Application of Flory's statistical theory for the estimation of internal pressure of liquid mixtures. *J. Chem. Res., Synop.* **2003**, 430–432.
- (39) Boned, C.; Zéberg-Mikkelsen, C. K.; Baylaucq, A.; Daugé, P. Highpressure dynamic viscosity and density of two synthetic hydrocarbon mixtures representative of some heavy petroleum distillation cuts. *Fluid Phase Equilib.* 2003, 212, 143–164.
- (40) Pečar, D.; Doleček, V. Volumetric properties of ethanol-water mixtures under high temperatures and pressures. *Fluid Phase Equilib.* 2005, 230, 36–44.
- (41) Verdier, S.; Andersen, S. I. Internal pressure and solubility parameter as a function of pressure. *Fluid Phase Equilib.* 2005, 231, 125– 137.
- (42) Moeini, V. A new regularity for internal pressure of dense fluids. J. Phys. Chem. 2006, 110, 3271–3275.
- (43) Melent'ev, V. V; Bolotnikov, M. F.; Neruchev, Y. A. Speeds of sound, densities, and isentropic compressibilities of 1-chlorohexane at temperatures from (293.15 to 413.15) K and pressures up to 200 MPa. J. Chem. Eng. Data 2006, 51, 181–185.
- (44) Moelwyn-Hughes, E. A. *Physical Chemistry*; Pergamon Press: London, 1961; 596 pp.
- (45) Kartsev, V. N.; Rodnikova, M. N.; Bartel, I.; Shtykov, S. N. The temperature dependence of internal pressure in liquids. *J. Phys. Chem.* 2002, 76, 1016–1018 (Russian).
- (46) Kartsev, V. N.; Rodnikova, M. N.; Shtykov, S. N. Inversion of the temperature coefficient of internal pressure and structural organization of liquid phase systems. *J. Struct. Chem.* **2004**, *45*, 91–95.
- (47) Kartsev, V. N.; Rodnikova, M. N.; Shtykov, S. N. On internal pressure, its temperature dependence, and the structure of liquid-phase systems. *J. Struct. Chem.* **2004**, *45*, 96–99.
- (48) Kartsev, V. N. To the understanding of the structural sensitivity of the temperature coefficient of internal pressure. J. Struct. Chem. 2004, 45, 832–837.
- (49) Randzio, S. L.; Grolier, J.-P. E.; Quint, J. R.; Eatough, D. J.; Lewis, E. A.; Hansen, L. D. n-Hexane as a model for compressed simple liquids. *Int. J. Thermophys.* **1994**, *15*, 415–441.

- (50) Randzio, S. L.; Grolier, J.-P. E.; Quint, J. R. Thermophysical properties of 1-hexanol over the temperature range from 303 K to 503 K and at pressures from the saturation line to 400 MPa. *Fluid Phase Equilib.* **1995**, *110*, 341–359.
- (51) Gumiński, K. Termodynamika; PWN: Warszawa, 1982; Chapter 2.4b.
- (52) Zorêbski, E.; Dzida, M. A study of the acoustic and thermodynamic properties of 1,2- and 1,3-butanediol by means of high-pressure speed

of sound measurements at temperatures from (293.15 to 318.15) K and pressures up to 101 MPa. J. Chem. Eng. Data (submitted).

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